

Since  $CE = 9$  and  $CB = 29$ ,  $\Delta s CE'E, CAB$  are similar in ratio of 9 to 29

$$\text{So } EE' = \frac{9 \cdot 20}{29}$$

$$\text{and } CE' = \frac{9 \cdot 21}{29} = 9$$

$$\Rightarrow E'A = 21 - CE' = \frac{20 \cdot 21}{29}$$

$$\text{So } \tan x = \frac{EE'}{E'A} = \frac{9 \cdot 20}{29} \cdot \frac{29}{20 \cdot 21} = \frac{3}{7} \quad (\text{see figure})$$

$$\text{So } \tan x = \frac{3}{7} \quad \text{Note that since } EE' \parallel AB, EE' \perp E'A$$

Using the exact same train of logic, we can show that

$$\tan y = \frac{2}{5}$$

$$\text{Now } x + y + \theta = 90, \Rightarrow (x + y) + \theta = 90, \Rightarrow \theta = 90 - (x + y)$$

$$\text{So } \tan \theta = \tan(90 - (x + y)) = \cot(x + y) = \frac{1}{\tan(x + y)} \quad \text{Also, } \theta \text{ is positive}$$

and acute.

$$\text{Now } \tan(x + y) = \frac{\tan x + \tan y}{1 - \tan x \tan y} = \frac{\frac{3}{7} + \frac{2}{5}}{1 - \frac{6}{35}} = \frac{\frac{29}{35}}{\frac{29}{35}} = 1$$

$$\text{So } \tan \theta = \frac{1}{\tan(x + y)} = \frac{1}{1} = 1$$

since  $\theta$  is acute and positive, we have

$$\tan \theta = 1 \Rightarrow \theta = \boxed{45^\circ \text{ or } \frac{\pi}{4} \text{ rad}}$$